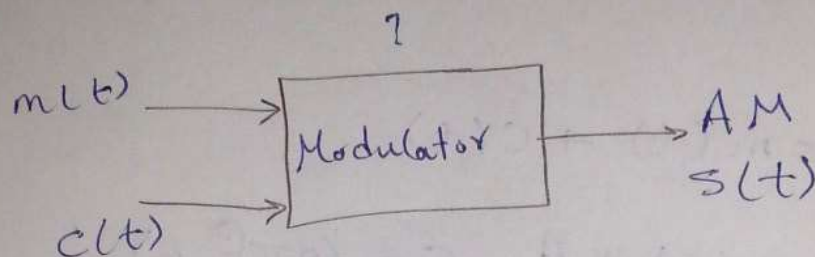


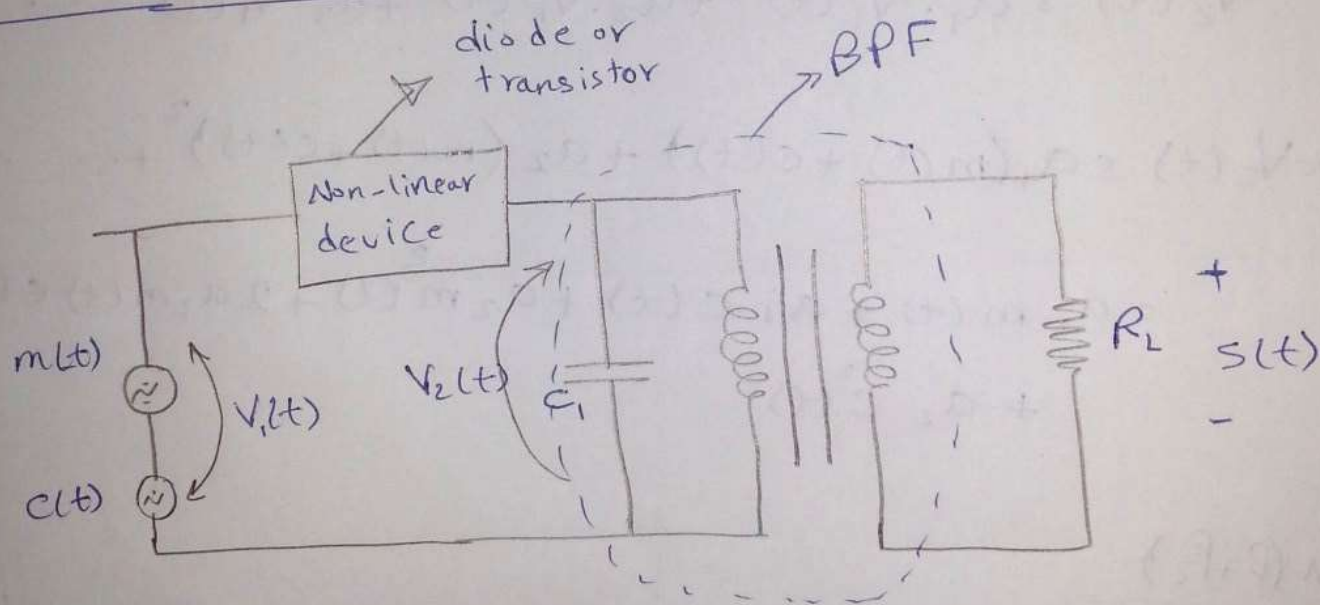
دقیقاً
✓ سہ

① Am Generation

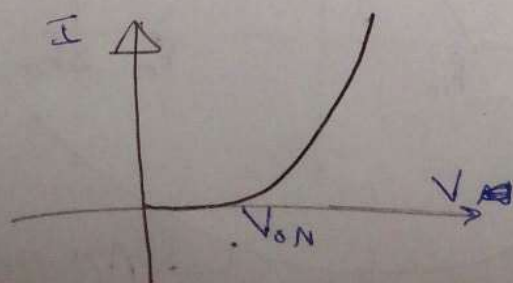
At Tx



① Square-law modulator



Generation & Detection



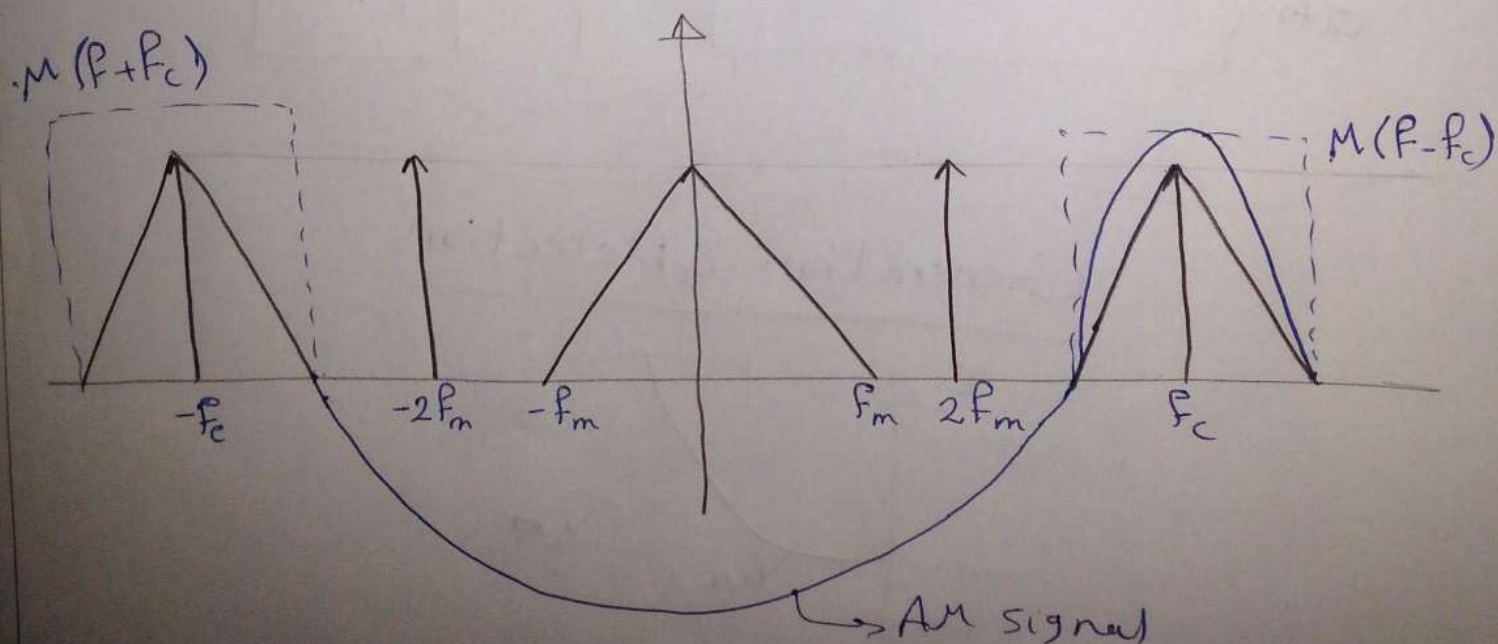
* Non Linear device: the relation between its voltage & current is non-linear (e.g. diode, transistor)

$$* V_1(t) \propto m(t) + c(t) \\ = m(t) + A_c \cdot \cos(2\pi f_c t)$$

$$* V_2(t) \propto a_1 \cdot V_1(t) + a_2 \cdot V_1^2(t) + a_3 \cdot V_1^3(t) + \dots$$

$$* V_2(t) \propto a_1(m(t) + c(t)) + a_2(m(t) + c(t))^2 + \dots$$

$$= a_1 m(t) + a_1 c(t) + a_2 m^2(t) + 2a_2 m(t)c(t) + a_2 c^2(t)$$



$$m^2(t) = A_m^2 \cos^2(2\pi f_m t)$$

$$m(t) = A_m \cos(2\pi f_m t)$$

$$m^2(t) = \frac{A_m^2}{2} (1 + \cos(4\pi f_m t))$$

$$M^2(f) = \frac{A_m^2}{2} \cdot \delta(f)$$

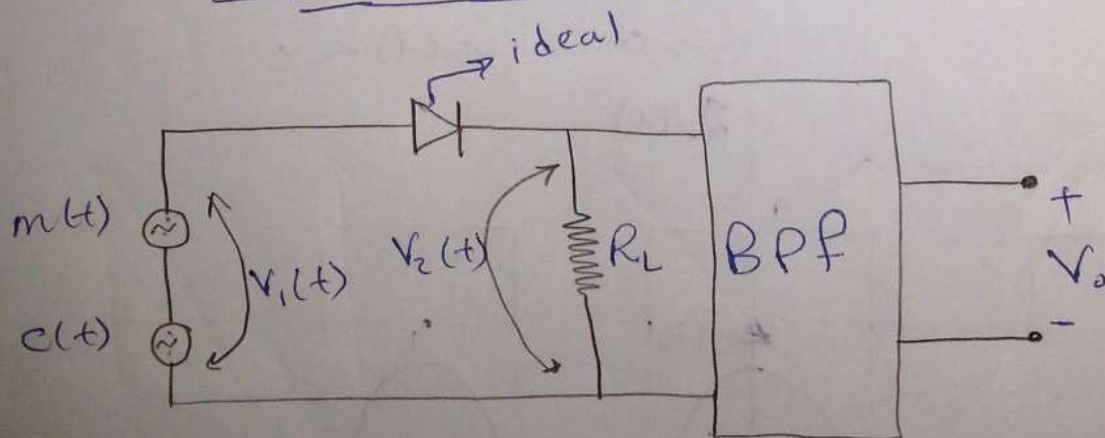
After BPF

$$s(t) = a_1 \cdot c(t) + 2a_2 \cdot m(t) \cdot c(t)$$

$$= a_1 \cdot A_c \cdot \cos(2\pi f_c t) + 2a_2 m(t) \cdot A_c \cdot \cos(2\pi f_c t)$$

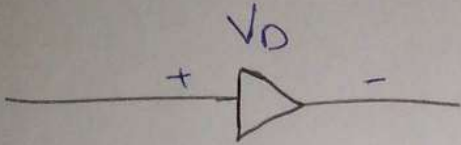
$$= a_1 \cdot A_c \left(1 + \frac{2a_2}{a_1} m(t)\right) \cos(2\pi f_c t)$$

[2] switching modulator



$$V_1(t) \sin(t) + c(t) \approx c(t)$$

$$M < 1 \rightarrow M = \frac{A_m}{A_c} \rightarrow A_m < A_c$$



if: $V_D > 0 \rightarrow$ Diode on (s.c)

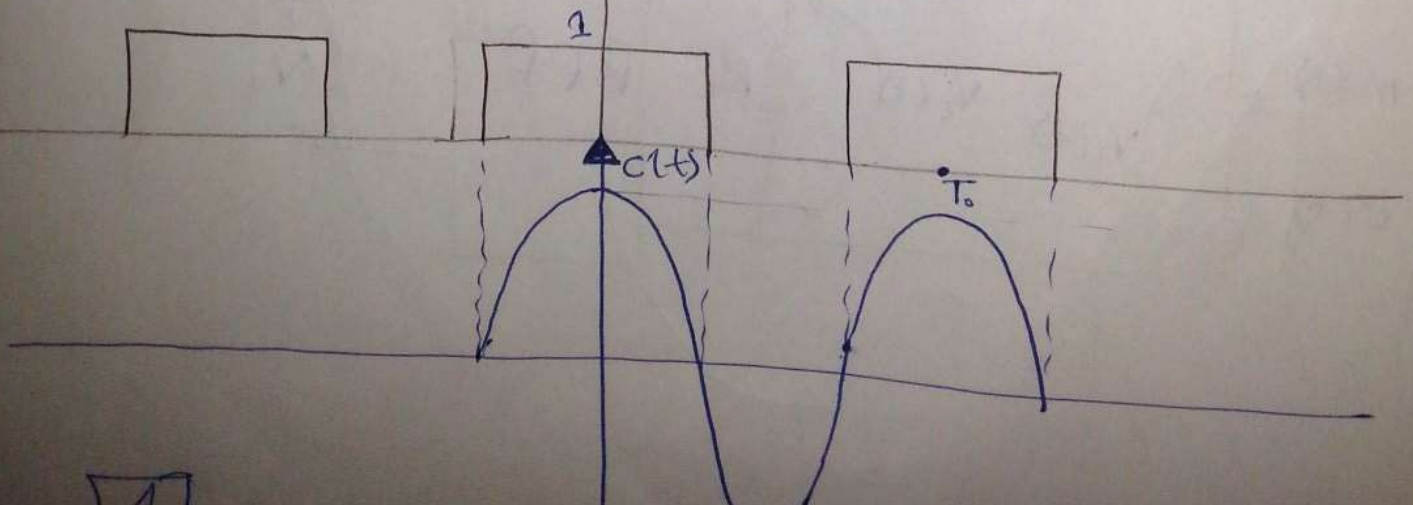
if: $V_D < 0 \rightarrow$ Diode off (o.c)

$$V_2(t) = \begin{cases} V_1(t) & , c(t) > 0 \\ 0 & , c(t) < 0 \end{cases}$$

$$* V_2(t) = V_1(t) * g_p(t)$$

$$\begin{cases} \rightarrow 1 & c(t) > 0 \\ \rightarrow 0 & c(t) < 0 \end{cases}$$

$\Delta g_p(t)$



$$g_p(t) = \frac{1}{2} + \frac{2}{\pi} \cos(2\pi f_c t) + \dots$$

$$V_2(t) = V_1(t) \cdot \left[\frac{1}{2} + \frac{2}{\pi} \cos(2\pi f_c t) + \dots \right]$$

$$= (m(t) + c(t)) \left[\frac{1}{2} + \frac{2}{\pi} \cos(2\pi f_c t) + \dots \right]$$

$$= \frac{1}{2} m(t) + \frac{1}{2} c(t) + \frac{2}{\pi} m(t) \cos(2\pi f_c t) +$$

$$\frac{2}{\pi} c(t) \cos(2\pi f_c t) + \dots$$

* After BPF

$$V_o = \frac{1}{2} c(t) + \frac{2}{\pi} m(t) \cdot \cos(2\pi f_c t)$$

$$= \frac{1}{2} \cdot A_c \cdot \cos(2\pi f_c t) + \frac{2}{\pi} m(t) \cos()$$

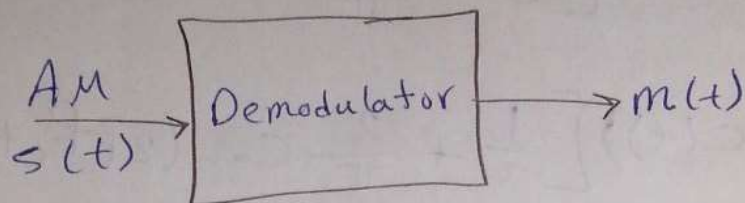
$$V_o = \frac{1}{2} A_c \left(1 + \frac{4 \cdot m(t)}{\pi A_c} \right) \cos(2\pi f_c t)$$

$$s(t) = A_c (1 + K_a \cdot m(t) \cos())$$

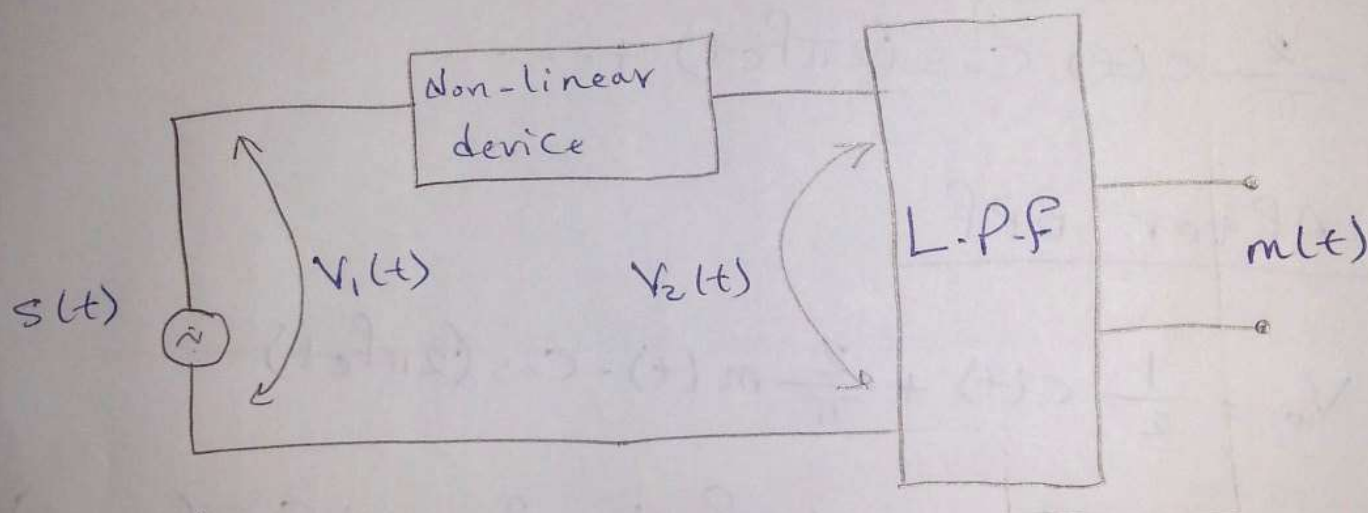
$$K_a = \frac{4}{\pi A_c}$$

Demodulator

At Rx



[I] Square-law demodulator



$$s(t) = V_1(t)$$

$$= A_c (1 + K_a \cdot m(t)) \cdot \cos(2\pi f_c t)$$

$$V_2(t) = a_1 \cdot A_c (1 + K_a \cdot m(t)) \cdot \cos(2\pi f_c t)$$

$$+ a_2 \cdot A_c^2 (1 + K_a \cdot m(t))^2 \cdot \cos^2(2\pi f_c t) - \dots$$

$$\rightarrow V_2(t) = a_1 \cdot V_1(t) + a_2 V_1^2(t) + \dots$$

$$V_2(t) = a_1 \cdot A_c (1 + K_a m(t)) \cos(2\pi f_c t)$$

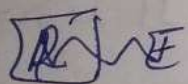
$$+ a_2 \cdot A_c^2 (1 + 2K_a \cdot m(t) + m^2(t)) \cos(4\pi f_c t)$$

$$\frac{1}{2} (1 + \cos(4\pi f_c t)) \dots$$

after LPF

$$V_o(t) = a_2 \cdot A_c^2 \cdot 2K_a \cdot \frac{1}{2} m(t)$$

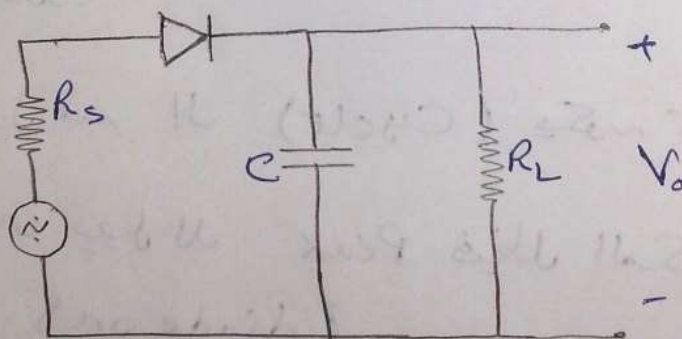
$$= a_2 \cdot A_c^2 \cdot K_a \cdot m(t)$$



* Envelope detector

Source signal

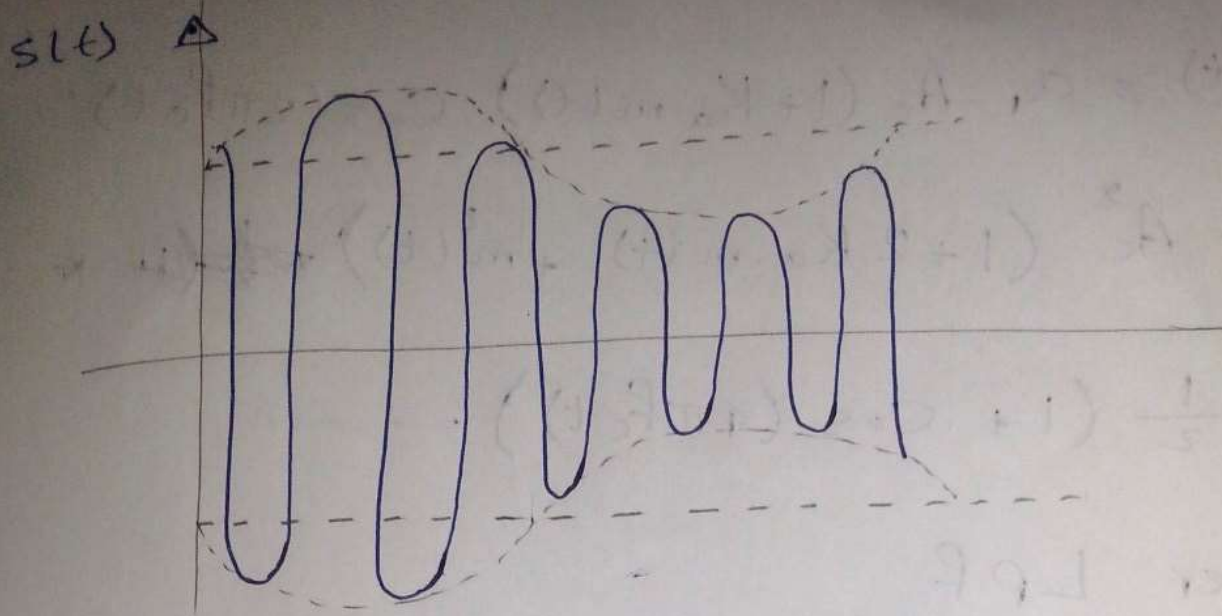
AM
wave



→ Envelope detector consists of

① diode

② R-c Filter



$s(t)$
 $v_r(t)$
 ← في البداية الـ $s(t)$ فلو كانت موجبة ،
 يكون الـ (diode on) ويوصل S-c والمكثف يشحن
 حتى يصل لهذا العدد .

* في الربع الأول منه الـ (Cycle) يكون كل نقطة أعلى
 منه اللي قبلها حتى يصل لـ Peak فيظل المكثف يشحن
 طالما الـ (diode on) .

* بعد الـ (Peak) تكون النقطة اللي بعدها أقل عنها
 $\text{Peak} < \text{Peak}$ فيوصل الـ (diode open) والمكثف يفرغ
 في المقاومة حتى يشحن مرة أخرى لما يرجع الجهد يزيد .

Note

$$\tau_{\text{charge}} = R_s \cdot C$$

* if τ is high value, C will need much time to charge.

$$R_s \cdot C \ll \boxed{\frac{1}{f_c}} \rightarrow \begin{array}{l} \text{الزمن الذي} \\ \text{Carrier} \\ \text{Carrier} \end{array}$$

← المطلوب؟ ~ يكون الشحنة سريع .

$$* \tau_{\text{discharge}} = R_L \cdot C$$

$$\frac{1}{f_c} \ll R_L \cdot C \ll \frac{1}{f_m}$$

~~Sheet 31~~

[9] Sec 7